Introduction to Exhaustible and Renewable Resources Lecture 3-1 of Policy and Planning Science in English

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Last lecture presented Robert Solow's seminal growth model, including the solution, comparative static and dynamic analysis. This lecture considers a model of a renewable resource, whose mathematical expression is quite similar to Solow's model, but whose in-Stephen J. Turnbull Exhaustible Resources

- Solow's basic *growth model* is entirely dynamic. No optimization is present at all.
- The "Golden Rule" is determined by using steady state to reduce the growth model to a single period (although it is repeated indefinitely), and then treating *s* as a choice variable in a *static* optimization.
- Now we look at *exhaustible resources*, both
 - renewable resources (concentrating on the fishery), and then
 - pure exhaustible resources (such as oil),

as first examples where economic considerations (optimization and equilibrium) enter.

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Pure Exhaustible Resources and Renewable Resources

- Exhaustible resources come in two varieties: *pure exhaustible resources* like oil, and *renewable resources* like fish. *Renewable resources* are "self-renewing" in that if left alone they will grow back to the original stock. However, like pure exhaustible resources (and unlike capital) there is an upper bound on the stock.
- Biological resources like fish are also similar to pure exhaustible resources in that once exhausted, there will never be any more (Jurassic Park excluded).
- Exhaustible resources are necessarily *storable*. Such resources have the property that the rental price (price of consumption) is equal to the asset price. (Compare: is the price of a rental car equal to purchase?)
- You might think that a pure exhaustible resource is just a special case of renewable resource, with the *natural rate of increase* set to zero. In some ways this is true, but each type has its own natural mode of analysis.

Summary: Exhaustible Resource Definition

- An *exhaustible resource* is a good where the stock is bounded and the natural rate of increase has an upper bound, but can be consumed arbitrarily quickly. If completely depleted, no more will ever exist.
 - A *pure exhaustible resource* cannot increase at all. Once any portion is consumed, that quantity is gone forever.
 - A *renewable resource* is an economic good whose stock automatically renews itself at some rate, but this rate (and the stock itself) has some upper bound.
- Renewable resources would better called *self-renewing* resources, but *renewable* is traditional usage and can't really be changed now.

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Examples of Exhaustible Resources

- A *pure exhaustible resource* can only be used up; it cannot increase. Oil (or any other mineral resource) is a good, and very important, example of a *pure* exhaustible resource.
- A *renewable resource* is one which has a positive *rate of natural increase*, for at least some level of the stock. Tuna fish (or any other wild biological resource) is an example.
- Solar energy is often called a "renewable energy source." That is reasonable English usage, but solar energy is not a *renewable resource* in the sense used here.
 - The Sun will always be there again tomorrow (no exhaustion).
 - It provides more energy than we can imagine using in the foreseeable future if only we could capture it (effectively unbounded).
- A habitat's "ability to absorb pollutants" may be analyzed as a renewable resource. Consider how Lake Erie (U.S.) or Lake Kasumigaura managed to recover from heavy pollution.

Introduction to Renewable Resources

- Dasgupta and Heal (*Economic Theory and Exhaustible Resources*, 1979) describe these as "resources that are at the same time self-renewable and *in principle* exhaustible."
- Not mineral resources, called "exhaustible," whose stock cannot be increased, although more efficient technology (*e.g.*, deeper oil wells) and discoveries of new stocks may arise.
- Not durable commodities. If the entire stock of automobiles were destroyed, we could still build more and replace them. This might depend on available exhaustible resources, but if the resources were available, the automobiles could be replaced.
- Populations of biological creatures, and agricultural land, are examples. Self-cleansing of polluted water is an example.

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- We borrow terms and ideas from biology, but the exact definitions used often differ.
- A *population* is a group of individuals of the same kind which reproduce themselves, perhaps only in the context of the group. The *population size* is the number of individuals. (In biology, it is often the *total mass*, because as resources become strained individual size decreases. We abstract from this issue.)
- In nature populations tend to increase over time. This increase should depend on
 - the period of time $\boldsymbol{\theta}$ over which increase is measured
 - the current population Z_t
 - other factors ζ_t

giving $Z_{t+\theta} = G(Z_t, \zeta_t, \theta)$.

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Typical Laws of Increase

- We are typically interested in the *natural rate of increase* of a population.
- If ζ is constant, then we may drop its notation. We typically assume that θ enters multiplicatively, and we write $G(Z_t, \theta) = Z_t + H(Z_t)\theta$.
- With continuous time, we rewrite as the difference, divide by θ , and take the limit as $\theta \to 0$:

$$\lim_{\theta \to 0} \frac{Z_{t+\theta} - Z_t}{\theta} = \dot{Z}_t = H(Z_t).$$

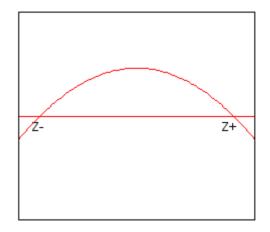
This *defines* H.

- Example: $H(Z) \equiv 0$ is a constant population size. This means renewable resources include exhaustible resources as a special case.
- Example: with abundant resources, $H(Z) = \lambda Z$, giving exponential growth.

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• Example: often, H(Z) is a bell curve.

Bell-Shaped Curves

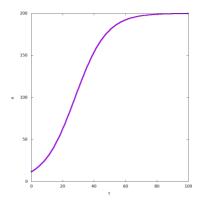


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The "S-shaped" logistic growth curve is a typical time path for a bell-shaped natural rate of increase function (in logistic growth, H(Z) =aZ(1-bZ), an inverted parabola.



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- We described pure exhaustible resources as a boundary case of renewable resources.
- Although we can use the same specifications to describe them, the mathematical analysis of the typical case often doesn't hold for the boundary case.
- Example: linear functions are a special case of convex functions. But a linear cost function doesn't allow us to determine the scale of firms in the industry—it doesn't matter if there is one firm or many, the cost structure is the same. However, strictly convex costs (decreasing returns to scale) will have a unique scale for each firm in equilibrium.

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Harvesting the Fishery

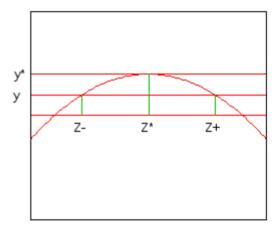
- How does the dynamic of the fishery change when we add large-scale fishing to the model?
- In economics, we simply remove fish from the population. In a differential equation model, we represent this by the rate of harvest at each instant of time, and write

$$\dot{Z}_t = H(Z_t) - y_t.$$

- In biology, we would also consider
 - Collateral damage to predators and prey of the commercially valuable fish. For example, tuna nets often catch (and drown) dolphins.
 - Pollution from fishing activity (*e.g.*, spilled oil and gasoline) might kill the target fish.
 - Fishing activity might interfere with reproduction.

Our simple model ignores these factors but they could be added.

Consider the stationary policy $y_t = y \le \tilde{y} = \max H$ for all *t*. Note that there are two steady states at Z^- (unstable) and Z^+ (stable), unless $y = \tilde{y}$, when the unique steady state at \tilde{Z} is *unstable*.



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- When $y = \tilde{y}$ there is a steady state at \tilde{Z} which is considered *unstable*.
- Looking closely, we see that although for $Z < \tilde{Z}$ where $\dot{Z} = H(Z) y < 0$ and Z diverges from \tilde{Z} , for $Z > \tilde{Z}$ again $\dot{Z} = H(Z) y < 0$, and Z converges to \tilde{Z} .
- Couldn't we say Z̃ is "half-stable" or "stable from the right"? Formally, yes, but as a model it doesn't make sense. We don't know why we deviate from Z̃, so it could be up or down. Eventually it will be down, and divergence will occur. If it reaches <u>Z</u>, extinction occurs (divergence is *permanent*).
- Conceptually (*i.e.*, in modeling) "stable" means "always converges." This approach is *useful* in modeling because we may assume that once the steady state is reached, the system will be "approximately in steady state" *forever*.

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Harvest Policy in a Feedback Loop

- The fact that the maximum harvest steady state is unstable means that a *laissez faire* policy toward the fishery is very *risky*. A policy which ignores the population and simply takes the optimal catch will eventually lead to extinction.
- Use the policy $y_t = \tilde{y} + \xi(Z_t \tilde{Z})$ to achieve a stable maximum harvest steady state.
 - This policy is called a *negative feedback loop*. The path of Z it induces is a *closed-loop solution*. (It's *negative* because in Z phase space we have

$$\dot{Z} = H(Z) - h(y) = H(Z) - (\tilde{y} + \xi(Z - \tilde{Z}))$$

so the direct coefficient on Z is $-\xi$.)

- The constant policy is called an *open-loop solution* (generally, any policy which is not a function of Z).
- Note that, though simple to state, this is not necessarily an easy policy to implement: how do you count the tuna in the sea? If many fisherman are involved, how do you share the cost of the census?

Closed-Loop Harvesting

y* У Z-Z* Z+

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Use the negative feedback policy $y_t = \tilde{y} + \xi(Z_t - \tilde{Z})$. Note that the steady state at maximum harvest is stable.

Comparing Solow's model with the fishery

- In Solow's model, the characteristic equation results in a bell curve, intersecting the horizontal axis (meaning k = 0, a steady state) at the origin and at some level of the capital-labor ratio, k*. The steady state at 0 is unstable, while the steady state at k* > 0 is stable.
- Similarly, in the fishery, the *natural rate of increase* curve is H a bell curve, intersecting the horizontal axis (meaning $\dot{Z} = H(Z) = 0$, a *steady state*) at $\underline{Z} \ge 0$ and at $\overline{Z} > \underline{Z}$. The steady state at \underline{Z} is *unstable*, while the steady state at \overline{Z} is *stable*.
- The difference between the two models is that in the fishery, H(Z) can be converted directly to consumption by harvesting the fish, which means that the maximum of H, $H(\tilde{Z})$ is of economic interest as the maxumim sustainable catch. On the other hand, \dot{k} is not even an input into production (k is), so it is not of economic interest in itself.

When Do Steady-State Policies Make Sense?

- This is an *economic* (not "purely dynamic" as with Solow) issue. Need an objective to optimize (until now, implicitly "maximize steady state y").
- Need an infinite planning horizon, else you want to use up the population "before the world ends."
- Entry must be controlled (else "tragedy of the commons" occurs as new entrants try to "grab their share" by consuming earlier than future entrants do).
- How about "maximum sustainable" harvest \tilde{y} (with a closed-loop policy)?
 - No discounting, or time preference outweighs higher future consumption.
 - With discounting, a steady-state optimal policy exists on the left side of the bell, with $Z < \tilde{Z}$.

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- The blue whales were hunted to near extinction (in the conservationist sense) by the early 1960s.
- We have a lot of data (appended) from the Committee for Whaling Statistics of Norway.
- Looking at the data we see that efficiency of catch was greatest in the 1930s, by the late 1950s was much less efficient.
- We can also see that the numbers are hardly smoothly varying, it's hard to see a clear trend, other than the average productivity.

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- So we see that the Japanese, Icelanders, and Norwegians argued that $Z_0 \geq \tilde{Z} > \underline{Z}$.
- The conservationists (and the non-whaling nations) worried that $Z_0 < \underline{Z}$, that is $Y = F(Z, X^*(Z)) > H(Z)$ for all Z
 - F(Z, X) is the catch of whales as a function of number of whales and number of ships in the industry (production function), and $X^*(Z)$ is the zero-profit number of ships as a function of Z (competitive equilibrium).
- Theoretically, it's impossible to say which is correct; we look at an empirical model.

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An Empirical Model

Using a discrete model, we have

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$$Z_{t+1} - Z_t = H(Z_t) = Z_t^{\alpha}(A - Z_t^{1-\alpha})$$
, and
• $Y_t = F(Z_t, X_t) = AZ_t^{\alpha}(1 - e^{-\nu X_t})$.

• Based on the data, we can estimate this system of equations (done by Michael Spence). We get

$$\nu = 0.0019, \quad \alpha = 0.8204, \quad A = 8.356.$$

• Maximum sustainable catch $H(\hat{Z}) = 9890$, while $\hat{Z} = 45177$.

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Are the Whales Endangered?

- Using $Y_{1960} = 1987$ and $X_{1960} = 418$, we get an estimate of $Z_{1960} = 1639$. That is, at that pace the whales would be extinct in the end of 1960! (Estimating for 1955-1959 gives Y = 1636, 1496, 1651, 1105, and 1174 respectively.)
- These numbers are pretty suspicious: they claim that for five years running whalers took more whales than were in the ocean.
- The implied natural rates of increase are pretty impressive, though: H(Z) = 1983, 1867, 1995, 1518, 1582, and 1985. Note that these track the catch numbers quite closely. This is not surprising: the model is tuned that way.

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- Our model implies that the whales are not below \underline{Z} , but well below Z^* .
- In fact, the calculation of the optimal policy suggests (using the figures above and r = 0.05) a period of abstaining for 9 years.
- $Z^* = 67000$, and $H(Z^*) = 9000$.
- History showed that political aspects are extremely important.

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Year	Boats	Catch	Year	Boats	Catch	Year	Boats	Catch
1909	149	316	1920	112	2987	1931	100	6705
1910	178	704	1921	142	5275	1932	186	19067
1911	251	1739	1922	174	6869	1933	199	17486
1912	246	2417	1923	194	4845	1934	242	16384
1913	254	2968	1924	234	7548	1935	312	18108
1914	182	4527	1925	235	7229	1936	254	14636
1915	151	5302	1926	233	8722	1937	357	15035
1916	94	4351	1927	222	9676	1938	362	14152
1917	130	2502	1928	242	13792			
1918	141	1993	1929	337	18755			
1919	154	2274	1930	280	26649			

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Whaling Data (post-WWII)

Year	Boats	Catch	Year	Boats	Catch
1945	158	3675	1953	368	3009
1946	246	9302	1954	386	2495
1947	307	7157	1955	419	1987
1948	348	7781	1956	395	1775
1949	382	6313	1957	417	1995
1950	468	7278	1958	420	1442
1951	430	5436	1959	399	1465
1952	379	4218	1960	418	1987

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Conclusions

- Profit maximization is consistent with some degree of conservation; it does not imply extinction of the species.
 Population will be smaller than Z
 , but greater than 0 in the steady state.
- If population is depleted below the optimal stationary policy, a profit-maximizing industry would advocate a total ban on harvesting, just like the conservationists!
- The maximum sustainable rate is not a focal point for policy.
- If $\tilde{Z} < \underline{Z}$, profit maximization conflicts with conservation.
- Also, things may be somewhat harsher than it seems here: in the long run, as supply of output falls, you might expect that q would rise, causing harvest rates to rise.
- $\tilde{Z} < \hat{Z}$.

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